

OXFORD CAMBRIDGE AND RSA EXAMINATIONS

**Advanced Subsidiary General Certificate of Education
Advanced General Certificate of Education**

MATHEMATICS

2637

Mechanics 1

Thursday

23 MAY 2002

Afternoon

1 hour 20 minutes

Additional materials:

Answer booklet

Graph paper

List of Formulae (MF8)

TIME 1 hour 20 minutes

INSTRUCTIONS TO CANDIDATES

- Write your Name, Centre Number and Candidate Number in the spaces provided on the answer booklet.
- Answer **all** the questions.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question or is clearly appropriate.
- Where a numerical value for the acceleration due to gravity is needed, use 9.8 m s^{-2} .
- You are permitted to use a graphic calculator in this paper.

INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [] at the end of each question or part question.
- The total number of marks for this paper is 60.
- Questions carrying smaller numbers of marks are printed earlier in the paper, and questions carrying larger numbers of marks later in the paper.
- **You are reminded of the need for clear presentation in your answers.**

This question paper consists of 4 printed pages.

1



An engine pulls a truck of mass 6000 kg along a straight horizontal track, exerting a constant horizontal force of magnitude E newtons on the truck (see diagram). The resistance to motion of the truck has magnitude 400 N, and the acceleration of the truck is 0.2 m s^{-2} . Find the value of E . [4]

2

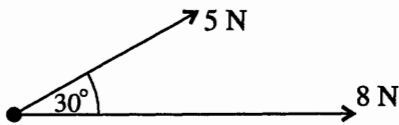


Fig. 1

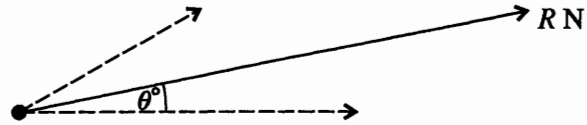
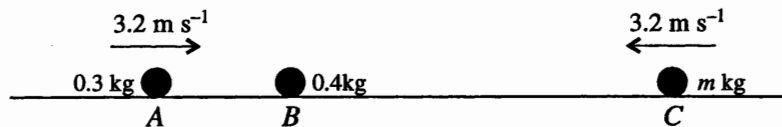


Fig. 2

Forces of magnitudes 8 N and 5 N act on a particle. The angle between the directions of the two forces is 30° , as shown in Fig. 1. The resultant of the two forces has magnitude R N and acts at an angle θ° to the force of magnitude 8 N, as shown in Fig. 2. Find R and θ . [7]

3



Three uniform spheres A , B and C have masses 0.3 kg, 0.4 kg and m kg respectively. The spheres lie in a smooth horizontal groove with B between A and C . Sphere B is at rest and spheres A and C are each moving with speed 3.2 m s^{-1} towards B (see diagram). Air resistance may be ignored.

(i) A collides with B . After this collision A continues to move in the same direction as before, but with speed 0.8 m s^{-1} . Find the speed with which B starts to move. [4]

(ii) B and C then collide, after which they both move towards A , with speeds of 3.1 m s^{-1} and 0.4 m s^{-1} respectively. Find the value of m . [4]

4 A particle is projected vertically upwards, from the ground, with a speed of 28 m s^{-1} . Ignoring air resistance, find

(i) the maximum height reached by the particle, [2]

(ii) the speed of the particle when it is 30 m above the ground, [3]

(iii) the time taken for the particle to fall from its highest point to a height of 30 m, [3]

(iv) the length of time for which the particle is more than 30 m above the ground. [1]

5 A particle P moves in a straight line so that, at time t seconds after leaving a fixed point O , its acceleration is $-\frac{1}{10}t \text{ m s}^{-2}$. At time $t = 0$, the velocity of P is $V \text{ m s}^{-1}$.

(i) Find, by integration, an expression in terms of t and V for the velocity of P . [3]

(ii) Find the value of V , given that P is instantaneously at rest when $t = 10$. [2]

(iii) Find the displacement of P from O when $t = 10$. [4]

6

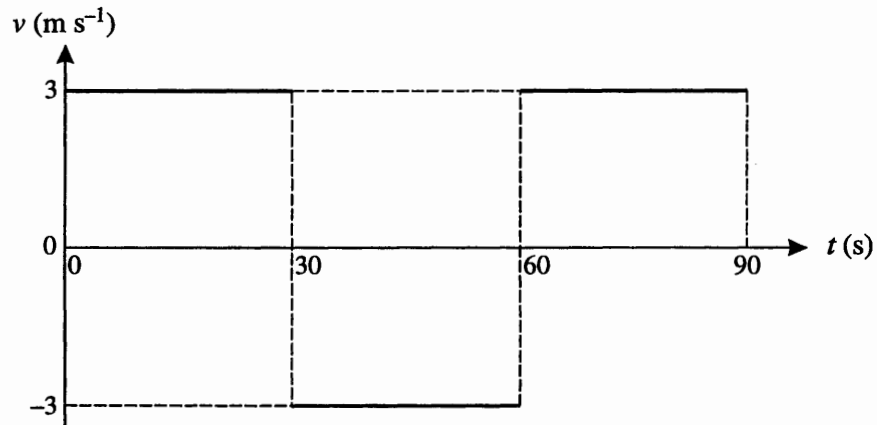


Fig. 1

A woman runs from A to B , then from B to A and then from A to B again, on a straight track, taking 90 s. The woman runs at a constant speed throughout. Fig. 1 shows the (t, v) graph for the woman.

(i) Find the total distance run by the woman. [2]

(ii) Find the distance of the woman from A when $t = 50$ and when $t = 80$. [3]

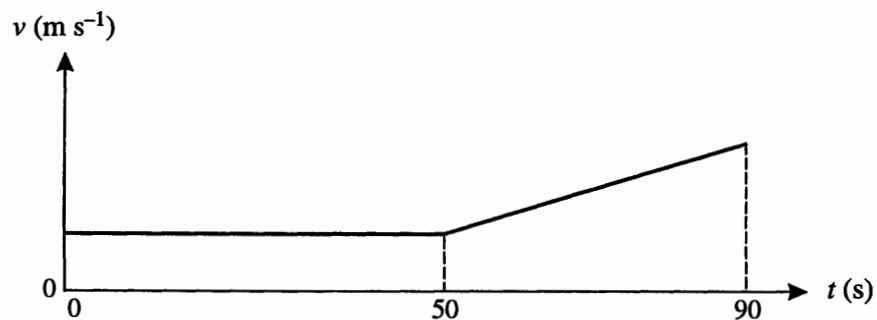


Fig. 2

At time $t = 0$, a child also starts to move, from A , along AB . The child walks at a constant speed for the first 50 s and then at an increasing speed for the next 40 s. Fig. 2 shows the (t, v) graph for the child; it consists of two straight line segments.

(iii) At time $t = 50$, the woman and child pass each other, moving in opposite directions. Find the speed of the child during the first 50 s. [3]

(iv) At time $t = 80$, the woman overtakes the child. Find the speed of the child at this instant. [3]

- 7 A sledge of mass 25 kg is on a plane inclined at 30° to the horizontal. The coefficient of friction between the sledge and the plane is 0.2.

(i)

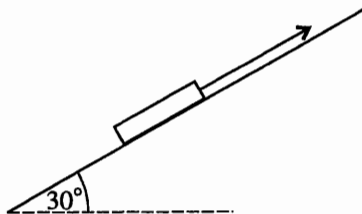


Fig. 1

The sledge is pulled up the plane, with constant acceleration, by means of a light cable which is parallel to a line of greatest slope (see Fig. 1). The sledge starts from rest and acquires a speed of 0.8 m s^{-1} after being pulled for 10 s. Ignoring air resistance, find the tension in the cable. [6]

(ii)

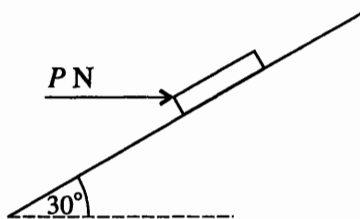


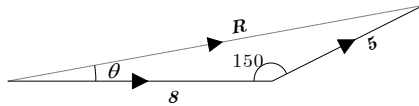
Fig. 2

On a subsequent occasion the cable is not in use and two people of total mass 150 kg are seated in the sledge. The sledge is held at rest by a horizontal force of magnitude P newtons, as shown in Fig. 2. Find the least value of P which will prevent the sledge from sliding down the plane. [6]

1 $N_2 \rightarrow E - 400 = 6000 \times 0.2 \quad E = 1600$

[4]

2



Cosine Rule

$$R^2 = 8^2 + 5^2 - 2 \times 8 \times 5 \times \cos 150^\circ = 158.2820\dots$$

$$R = 12.5810\dots = 12.6$$

Sine Rule

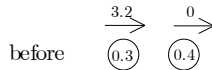
$$\frac{\sin \theta}{5} = \frac{\sin 150^\circ}{12.5810\dots}$$

$$\sin \theta = 0.1987\dots$$

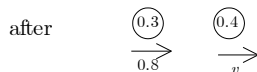
$$\theta = 11.4616\dots = 11.5^\circ$$

[7]

3



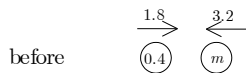
conservation of momentum



$$3.2 \times 0.3 + 0 = 0.8 \times 0.3 + 0.4v$$

$$v = 1.8 \text{ ms}^{-1}$$

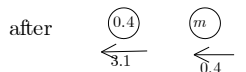
[4]



$$0.4 \times 1.8 + m \times (-3.2) = 0.4 \times (-3.1) + m \times (-0.4)$$

$$1.96 = 2.8m$$

$$m = 0.7$$



[4]

4 taking 'up' as positive....

$$v^2 = u^2 + 2as$$

$$0 = 28^2 - 2 \times 9.8 \times h_{\max}$$

$$h_{\max} = 40 \text{ m}$$

[2]

when 30 m above ground ...

$$v^2 = u^2 + 2as$$

$$v^2 = 28^2 - 19.6 \times 30 = 196$$

$$\text{speed} = 14 \text{ ms}^{-1}$$

[3]

time from top to 30 m ...

$$v = u + at$$

$$t = \frac{v - u}{a} = \frac{-14 - 0}{-9.8} = \frac{10}{7} \text{ s}$$

[3]

$$\text{time above 30 m} = 2 \times \frac{10}{7} = \frac{20}{7} = 2\frac{6}{7} \text{ s}$$

[1]

5

$$v = \int -\frac{1}{10} t \, dt = -\frac{1}{20} t^2 + c = V - \frac{1}{20} t^2$$

[3]

$$v \, 10 = 0 \quad \Rightarrow \quad V - \frac{1}{20} \times 10^2 = 0 \quad \Rightarrow \quad V = 5$$

[2]

$$s = \int_0^{10} v \, dt = \int_0^{10} 5 - \frac{1}{20} t^2 \, dt = \left[5t - \frac{1}{60} t^3 \right]_0^{10} = 50 - \frac{100}{6} = 33 \frac{1}{3} \text{ m}$$

[4]

6

total distance run by woman = $90 \times 3 = 270 \text{ m}$

[2]

$t = 50$ distance from A = $10 \times 3 = 30 \text{ m}$

$t = 80$ distance from A = $20 \times 3 = 60 \text{ m}$

[3]

speed of child in 1st phase = $\frac{30}{50} = 0.6 \text{ ms}^{-1}$

[3]

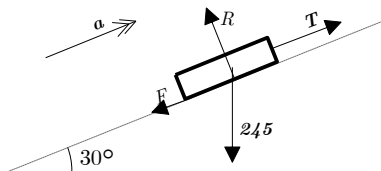
at $t = 80$, child has covered 60 m in total; that is, 30 m in 2nd phase.

for the first 30 s of 2nd phase

$$s = \left(\frac{u + v}{2} \right) t \quad \Rightarrow \quad 30 = \left(\frac{0.6 + v}{2} \right) 30 \quad \Rightarrow \quad v = 1.4 \text{ ms}^{-1}$$

[3]

7



$$v = u + at \quad a = \frac{v - u}{t} = \frac{0.8}{10} = 0.08$$

$$\text{N2 normal to slope} \quad R - 245 \cos 30^\circ = 0$$

$$R = 212.1762\dots$$

limiting

friction ...

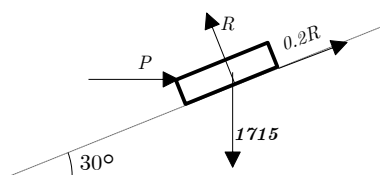
$$F = \mu R = 42.4352\dots$$

N2 up the slope

$$T - 42.4352 - 245 \sin 30^\circ = 25 \times 0.08$$

$$T = 166.935\dots = 167 \text{ N}$$

[6]



$$\left. \begin{array}{l} \text{N2 parallel} \quad 0.2R - P \cos 30^\circ = 1715 \sin 30^\circ \\ \text{N2 normal} \quad R - P \sin 30^\circ = 1715 \cos 30^\circ \end{array} \right\} \mu$$

$$P = \frac{1715 \cdot 5 \sin 30^\circ \cdot \cos 30^\circ}{\sin 30^\circ + 5 \cos 30^\circ} = 580.1641\dots = 580 \text{ (3 s.f.)}$$

[6]

Total [60]