

Paper Reference(s)

6691/01

Edexcel GCE

Statistics S3

Advanced Level

Friday 18 June 2010 – Afternoon

Time: 1 hour 30 minutes

Materials required for examination

Mathematical Formulae (Pink)

Items included with question papers

Nil

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulas stored in them.

Instructions to Candidates

In the boxes on the answer book, write the name of the examining body (Edexcel), your centre number, candidate number, the unit title (Statistics S3), the paper reference (6691), your surname, other name and signature.

Values from the statistical tables should be quoted in full. When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information for Candidates

A booklet 'Mathematical Formulae and Statistical Tables' is provided.

Full marks may be obtained for answers to ALL questions.

This paper has 7 questions.

The total mark for this paper is 75.

Advice to Candidates

You must ensure that your answers to parts of questions are clearly labelled.

You must show sufficient working to make your methods clear to the Examiner.

Answers without working may not gain full credit.

1. A report states that employees spend, on average, 80 minutes every working day on personal use of the Internet. A company takes a random sample of 100 employees and finds their mean personal Internet use is 83 minutes with a standard deviation of 15 minutes. The company's managing director claims that his employees spend more time on average on personal use of the Internet than the report states.

Test, at the 5% level of significance, the managing director's claim. State your hypotheses clearly.

(7)

2. Philip and James are racing car drivers. Philip's lap times, in seconds, are normally distributed with mean 90 and variance 9. James' lap times, in seconds, are normally distributed with mean 91 and variance 12. The lap times of Philip and James are independent. Before a race, they each take a qualifying lap.

(a) Find the probability that James' time for the qualifying lap is less than Philip's.

(4)

The race is made up of 60 laps. Assuming that they both start from the same starting line and lap times are independent,

(b) find the probability that Philip beats James in the race by more than 2 minutes.

(5)

3. A woodwork teacher measures the width, w mm, of a board. The measured width, X mm, is normally distributed with mean w mm and standard deviation 0.5 mm.

(a) Find the probability that X is within 0.6 mm of w .

(2)

The same board is measured 16 times and the results are recorded.

(b) Find the probability that the mean of these results is within 0.3 mm of w .

(4)

Given that the mean of these 16 measurements is 35.6 mm,

(c) find a 98% confidence interval for w .

(4)

4. A researcher claims that, at a river bend, the water gradually gets deeper as the distance from the inner bank increases. He measures the distance from the inner bank, b cm, and the depth of a river, s cm, at seven positions. The results are shown in the table below.

Position	A	B	C	D	E	F	G
Distance from inner bank b cm	100	200	300	400	500	600	700
Depth s cm	60	75	85	76	110	120	104

- (a) Calculate Spearman's rank correlation coefficient between b and s . (6)
- (b) Stating your hypotheses clearly, test whether or not the data provides support for the researcher's claim. Use a 1% level of significance. (4)
-

5. A random sample of 100 people were asked if their finances were worse, the same or better than this time last year. The sample was split according to their annual income and the results are shown in the table below.

Finances Annual income	Worse	Same	Better
Under £15 000	14	11	9
£15 000 and above	17	20	29

- Test, at the 5% level of significance, whether or not the relative state of their finances is independent of their income range. State your hypotheses and show your working clearly. (10)
-

6. A total of 228 items are collected from an archaeological site. The distance from the centre of the site is recorded for each item. The results are summarised in the table below.

Distance from the centre of the site (m)	0–1	1–2	2–4	4–6	6–9	9–12
Number of items	22	15	44	37	52	58

- Test, at the 5% level of significance, whether or not the data can be modelled by a continuous uniform distribution. State your hypotheses clearly. (12)
-

7. A large company surveyed its staff to investigate the awareness of company policy. The company employs 6000 full-time staff and 4000 part-time staff.

(a) Describe how a stratified sample of 200 staff could be taken. (3)

(b) Explain an advantage of using a stratified sample rather than a simple random sample. (1)

A random sample of 80 full-time staff and an independent random sample of 80 part-time staff were given a test of policy awareness. The results are summarised in the table below.

	Mean score (\bar{x})	Variance of scores (s^2)
Full-time staff	52	21
Part-time staff	50	19

(c) Stating your hypotheses clearly, test, at the 1% level of significance, whether or not the mean policy awareness scores for full-time and part-time staff are different. (7)

(d) Explain the significance of the Central Limit Theorem to the test in part (c). (2)

(e) State an assumption you have made in carrying out the test in part (c). (1)

After all the staff had completed a training course the 80 full time staff and the 80 part-time staff were given another test of policy awareness. The value of the test statistic z was 2.53.

(f) Comment on the awareness of company policy for the full-time and part-time staff in light of this result. Use a 1% level of significance. (2)

(g) Interpret your answers to part (c) and part (f). (1)

TOTAL FOR PAPER: 75 MARKS

END

June 2010
Statistics S3 6691
Mark Scheme

Question Number	Scheme	Marks
Q1	<p>$H_0: \mu = 80, H_1: \mu > 80$</p> $z = \frac{83 - 80}{\frac{15}{\sqrt{100}}} = 2$ <p>$2 > 1.6449$ (accept 1.645 or better)</p> <p>Reject H_0 <u>or</u> significant result <u>or</u> in the critical region Managing director's claim is supported.</p>	<p>B1,B1</p> <p>M1A1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p style="text-align: right;">7</p>
<p>2nd M1A1</p> <p>Critical Region</p>	<p>1st B1 for H_0. They must use μ not x, p, λ or \bar{x} etc</p> <p>2nd B1 for H_1 (must be > 80). Same rules about μ.</p> <p>1st M1 for attempt at standardising using 83, 80 and $\frac{15}{\sqrt{100}}$. Can accept \pm.</p> <p>May be implied by $z = \pm 2$</p> <p>1st A1 for + 2 only</p> <p>3rd B1 for ± 1.6449 seen (or probability of 0.0228 or better)</p> <p>2nd M1 for a correct statement about "significance" or rejecting H_0 (or H_1) based on their z value and their 1.6449 (provided it is a recognizable critical value from normal tables) <u>or</u> their probability (< 0.5) and significance level of 0.05. Condone their probability > 0.5 compared with 0.95 for the 2nd M1</p> <p>2nd A1 for a correct contextualised comment. Must mention "director" and "claim" <u>or</u> "time" and "use of Internet". No follow through.</p> <p>If no comparison or statement is made but a correct contextualised comment is given the M1 can be implied. If a comparison is made it must be <u>compatible</u> with statement otherwise M0 e.g. comparing 0.0228 with 1.6449 is M0 or comparing probability 0.9772 with 0.05 is M0 comparing -2 with - 1.6449 is OK provided a correct statement accompanies it condone -2 $>$ -1.6449 provided their statement correctly rejects H_0.</p> <p>They may find a critical region for \bar{X}: $\bar{X} > 80 + \frac{15}{\sqrt{100}} \times 1.6449 = \text{awrt } 82.5$</p> <p>1st M1 for $80 + \frac{15}{\sqrt{100}} \times (z \text{ value})$</p> <p>3rd B1 for 1.645 or better</p> <p>1st A1 for awrt 82.5</p> <p>The rest of the marks are as per the scheme.</p>	

Question Number	Scheme	Marks
Q2	<p style="text-align: center;">[$P \sim N(90,9)$ and $J \sim N(91,12)$]</p> <p>(a) $(J - P) \sim N(1, 21)$ $P(J < P) = P(J - P < 0)$ $= P\left(Z < \frac{0-1}{\sqrt{21}}\right)$ $= P(Z < -0.2182\dots)$ $= 1 - 0.5871 = 0.4129$ calculator (0.4136....)</p> <p>(b) $X = (J_1 + J_2 + \dots + J_{60}) - (P_1 + P_2 + \dots + P_{60})$ $E(X) = 60 \times 91 - 60 \times 90 = 60$ [stated as $E(X) = 60$ or $X \sim N(60, \dots)$] $\text{Var}(X) = 60 \times 9 + 60 \times 12 = 1260$ $P(X > 120) = P\left(Z > \frac{120-60}{\sqrt{1260}}\right)$ $= P(Z > 1.69030\dots)$ $= 1 - 0.9545 = 0.0455$</p>	<p>M1, A1</p> <p>dM1</p> <p>A1 (4)</p> <p>M1</p> <p>B1</p> <p>A1</p> <p>M1</p> <p>A1 (5)</p> <p style="text-align: right;">9</p>
Use of means	<p>(a) 1st M1 for attempting $J - P$ and $E(J - P)$ or $P - J$ and $E(P - J)$ 1st A1 for variance of 21 (Accept 9 + 12). Ignore any slip in μ here. 2nd dM1 for attempting the correct probability and standardising with their mean and sd. This mark is dependent on previous M so if $J - P$ (or $P - J$) is not being used score M0 If their method is not crystal clear then they must be attempting $P(Z < -ve \text{ value})$ or $P(Z > +ve \text{ value})$ i.e. their probability <u>after</u> standardisation should lead to a prob. < 0.5 so e.g. $P(J - P < 0)$ leading to 0.5871 is M0A0 unless the M1 is clearly earned. 2nd A1 for awrt 0.413 or 0.414</p> <p style="text-align: center;">The first 3 marks may be implied by a correct answer</p> <p>(b) 1st M1 for a clear attempt to identify a correct form for X. This may be implied by correct variance of 1260 B1 for $E(X) = 60$. Can be awarded even if they are using $X = 60J - 60P$. Allow $P - J$ and -60 1st A1 for a correct variance. If 1260 is given the M1 is scored by implication. 2nd M1 for attempting a correct probability and standardising with 120 and their 60 and 1260 If the answer is incorrect a full <u>expression</u> must be seen following through their values for M1 e.g. $P\left(Z > \frac{120 - \text{their } 60}{\sqrt{\text{their variance}}}\right)$. If using -60, should get $P\left(Z < \frac{-120 - -60}{\sqrt{\text{their variance}}}\right)$</p> <p>Attempt to use $\bar{J} - \bar{P}$ for 1st M1, $E(\bar{J} - \bar{P}) = 1$ for B1 and $\text{Var}(\bar{J} - \bar{P}) = 0.35$ for A1 Then 2nd M1 for standardisation with 2, and their 1 and 0.35</p>	

Question Number	Scheme	Marks
Q3 (a)	$E \sim N(0, 0.5^2)$ or $X \sim N(w, 0.5^2)$ $P(E < 0.6) = P\left(Z < \frac{0.6}{0.5}\right)$ or $P(X - w < 0.6) = P\left(Z < \frac{0.6}{0.5}\right)$ $= P(Z < 1.2)$ $= 2 \times 0.8849 - 1 = 0.7698$ awrt 0.770	M1 A1 (2)
(b)	$\bar{E} \sim N\left(0, \frac{1}{64}\right)$ or $\bar{X} \sim N\left(w, \frac{0.5^2}{16}\right)$ $P(\bar{E} < 0.3) = P\left(Z < \frac{0.3}{\frac{1}{8}}\right)$ or $P(\bar{X} - w < 0.3) = P\left(Z < \frac{0.3}{\frac{1}{8}}\right)$ $= P(Z < 2.4)$ $= 2 \times 0.9918 - 1 = 0.9836$ awrt 0.984	M1 M1, A1 A1 (4)
(c)	$35.6 \pm 2.3263 \times \frac{1}{8}$ (35.3, 35.9)	M1 B1 A1, A1 (4) 10
(a)	1 st M1 for identifying a correct probability (they must have the 0.6) and attempting to standardise. Need . This mark can be given for 0.8849 - 0.1151 seen as final answer. 1 st A1 for awrt 0.770. NB an answer of 0.3849 or 0.8849 scores M0A0 (since it implies no) M1 may be implied by a correct answer	
(b)	1 st M1 for a correct attempt to define \bar{E} or \bar{X} but must attempt $\frac{\sigma^2}{n}$. Condone labelling as E or X This mark may be implied by standardisation in the next line. 2 nd M1 for identifying a correct probability statement using \bar{E} or \bar{X} . Must have 0.3 and 1 st A1 for correct standardisation as printed or better 2 nd A1 for awrt 0.984 The M marks may be implied by a correct answer.	
Sum of 16, not means	1 st M1 for correct attempt at suitable sum distribution with correct variance ($= 16 \times \frac{1}{4}$) 2 nd M1 for identifying a correct probability. Must have 4.8 and 1 st A1 for correct standardisation i.e. need to see $\frac{4.8}{\sqrt{4}}$ or better	
(c)	M1 for $35.6 \pm z \times \frac{0.5}{\sqrt{16}}$ B1 for 2.3263 or better. Use of 2.33 will lose this mark but can still score $\frac{3}{4}$ 1 st A1 for awrt 35.3 2 nd A1 for awrt 35.9	

Question Number	Scheme	Marks																																
Q4 (a)	<table border="1" data-bbox="309 304 1238 555"> <tr><td>Distance rank</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td></tr> <tr><td>Depth rank</td><td>1</td><td>2</td><td>4</td><td>3</td><td>6</td><td>7</td><td>5</td></tr> <tr><td>d</td><td>0</td><td>0</td><td>1</td><td>1</td><td>1</td><td>1</td><td>2</td></tr> <tr><td>d^2</td><td>0</td><td>0</td><td>1</td><td>1</td><td>1</td><td>1</td><td>4</td></tr> </table> <p data-bbox="223 627 351 683">$\sum d^2 = 8$</p> <p data-bbox="223 689 526 862"> $r_s = 1 - \frac{6 \times 8}{7 \times 48}$ $= \frac{6}{7} = 0.857142$ </p> <p data-bbox="1145 801 1289 840">awrt 0.857</p>	Distance rank	1	2	3	4	5	6	7	Depth rank	1	2	4	3	6	7	5	$ d $	0	0	1	1	1	1	2	d^2	0	0	1	1	1	1	4	<p data-bbox="1353 421 1401 459">M1</p> <p data-bbox="1353 492 1401 530">M1</p> <p data-bbox="1353 631 1439 669">M1A1</p> <p data-bbox="1353 725 1401 763">M1</p> <p data-bbox="1353 819 1401 857">A1</p> <p data-bbox="1471 857 1519 896">(6)</p>
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$ d $	0	0	1	1	1	1	2																											
d^2	0	0	1	1	1	1	4																											
(b)	<p data-bbox="223 896 491 934">$H_0 : \rho = 0, H_1 : \rho > 0$</p> <p data-bbox="223 943 678 981">Critical value at 1% level is 0.8929</p> <p data-bbox="223 990 893 1028">$r_s < 0.8929$ so not significant evidence to reject H_0,</p> <p data-bbox="223 1037 877 1075">The researcher's claim is not correct (at 1% level).</p> <p data-bbox="223 1084 837 1122"><u>or</u> insufficient evidence for researcher's claim</p> <p data-bbox="223 1131 1252 1169"><u>or</u> there is insufficient evidence that water gets deeper further from inner bank.</p> <p data-bbox="223 1178 1284 1216"><u>or</u> no (positive) correlation between depth of water and distance from inner bank</p>	<p data-bbox="1353 896 1401 934">B1</p> <p data-bbox="1353 943 1401 981">B1</p> <p data-bbox="1353 990 1401 1028">M1</p> <p data-bbox="1353 1037 1423 1075">A1ft</p> <p data-bbox="1471 1075 1519 1113">(4)</p> <p data-bbox="1471 1178 1519 1216">10</p>																																
(a)	<p data-bbox="223 1240 1053 1279">1st M1 for an attempt to rank the depths against the distances</p> <p data-bbox="223 1288 1053 1326">2nd M1 for attempting d for their ranks. Must be using ranks.</p> <p data-bbox="223 1335 917 1373">3rd M1 for attempting $\sum d^2$ (must be using ranks)</p> <p data-bbox="223 1382 885 1420">1st A1 for sum of 8 (or 104 for reverse ranking)</p> <p data-bbox="223 1429 1508 1500">4th M1 for use of the correct formula with their $\sum d^2$. If answer is not correct an expression is required.</p> <p data-bbox="223 1509 1508 1547">2nd A1 for awrt (\pm) 0.857. Sign should correspond to ranking (so use of 104 should get -0.857)</p>																																	
(b)	<p data-bbox="223 1579 1508 1617">1st B1 for both hypotheses in terms of ρ, H_1 must be one tail and compatible with their ranking</p> <p data-bbox="223 1626 718 1664">2nd B1 for cv of 0.8929 (accept \pm)</p> <p data-bbox="223 1673 1428 1711">M1 for a correct statement relating their r_s with their cv but cv must be such that $cv < 1$</p> <p data-bbox="223 1720 1444 1861">A1ft for a correct contextualised comment. Must mention "researcher" and "claim" <u>or</u> "distance (from bank)" and "depth (of water)" Follow through their r_s and their cv (provided it is $cv < 1$) Use of "association" is A0</p>																																	

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Q5	<table border="1" data-bbox="220 291 1216 465"> <thead> <tr> <th>Finances</th> <th>Worse</th> <th>Same</th> <th>Better</th> <th></th> </tr> </thead> <tbody> <tr> <td>Income</td> <td></td> <td></td> <td></td> <td></td> </tr> <tr> <td>Under £15 000</td> <td>10.54</td> <td>10.54</td> <td>12.92</td> <td>34</td> </tr> <tr> <td>£15 000 and above</td> <td>20.46</td> <td>20.46</td> <td>25.08</td> <td>66</td> </tr> <tr> <td></td> <td>31</td> <td>31</td> <td>38</td> <td>100</td> </tr> </tbody> </table> <p data-bbox="220 510 1085 548">H_0 : State of finances and income are independent (not associated)</p> <p data-bbox="220 555 1085 593">H_1 : State of finances and income are not independent (associated)</p> <table border="1" data-bbox="220 638 826 967"> <thead> <tr> <th>O_i</th> <th>E_i</th> <th>$\frac{(O_i - E_i)^2}{E_i}$</th> <th>$\frac{O_i^2}{E_i}$</th> </tr> </thead> <tbody> <tr> <td>14</td> <td>10.54</td> <td>1.1358....</td> <td>18.59..</td> </tr> <tr> <td>11</td> <td>10.54</td> <td>0.0200....</td> <td>11.48..</td> </tr> <tr> <td>9</td> <td>12.92</td> <td>1.1893...</td> <td>6.269..</td> </tr> <tr> <td>17</td> <td>20.46</td> <td>0.5851...</td> <td>14.12..</td> </tr> <tr> <td>20</td> <td>20.46</td> <td>0.0103...</td> <td>19.55..</td> </tr> <tr> <td>29</td> <td>25.08</td> <td>0.6126...</td> <td>33.53..</td> </tr> </tbody> </table> <p data-bbox="220 990 1324 1075">$\sum \frac{(O_i - E_i)^2}{E_i} = 3.553... \quad \text{or} \quad \sum \frac{O_i^2}{E_i} - 100 = 103.553... - 100 = 3.553... \quad (\text{awrt } \mathbf{3.55})$</p> <p data-bbox="220 1079 486 1120">$\nu = (3 - 1)(2 - 1) = 2$</p> <p data-bbox="220 1124 359 1160">cv is 5.991</p> <p data-bbox="220 1169 1125 1209">3.553 < 5.991 so insufficient evidence to reject H_0 <u>or</u> not significant</p> <p data-bbox="220 1214 1173 1254">There is no evidence of association between state of finances and income.</p>	Finances	Worse	Same	Better		Income					Under £15 000	10.54	10.54	12.92	34	£15 000 and above	20.46	20.46	25.08	66		31	31	38	100	O_i	E_i	$\frac{(O_i - E_i)^2}{E_i}$	$\frac{O_i^2}{E_i}$	14	10.54	1.1358....	18.59..	11	10.54	0.0200....	11.48..	9	12.92	1.1893...	6.269..	17	20.46	0.5851...	14.12..	20	20.46	0.0103...	19.55..	29	25.08	0.6126...	33.53..	<p data-bbox="1353 380 1404 459">M1 A1</p> <p data-bbox="1353 542 1396 577">B1</p> <p data-bbox="1353 784 1404 819">M1</p> <p data-bbox="1353 855 1396 891">A1</p> <p data-bbox="1353 1019 1396 1055">A1</p> <p data-bbox="1353 1079 1396 1115">B1</p> <p data-bbox="1353 1124 1396 1160">B1</p> <p data-bbox="1353 1169 1396 1205">M1</p> <p data-bbox="1353 1214 1396 1249">A1</p> <p data-bbox="1476 1288 1516 1323">10</p>
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	<p data-bbox="220 1348 1252 1422">1st M1 for some use of $\frac{\text{Row Total} \times \text{Col.Total}}{\text{Grand Total}}$. May be implied by correct E_i</p> <p data-bbox="220 1429 805 1464">1st A1 for all expected frequencies correct</p> <p data-bbox="220 1467 1436 1541">B1 for both hypotheses. Must mention “state” or “finances” and “income” at least once Use of “relationship” or “correlation” or “connection” is B0</p> <p data-bbox="220 1541 1492 1579">2nd M1 for at least two correct terms (as in 3rd or 4th column) or correct expressions with their E_i</p> <p data-bbox="220 1585 1500 1624">2nd A1 for all correct terms. May be implied by a correct answer.(2 dp or better-allow eg 1.13...)</p> <p data-bbox="220 1630 1468 1668">3rd M1 for a correct statement linking their test statistic and their cv . Must be χ^2 not normal.</p> <p data-bbox="220 1675 1468 1780">4th A1 for a correct comment in context - must mention “state” or “finances” and “income” condone “relationship” or “connection” here but not “correlation”. No follow through. e.g. “There is no evidence of a relationship between finances and income”</p>																																																						

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Q6	<table border="1" data-bbox="220 309 1257 577"> <tr> <td>Distance from centre of site (m)</td> <td>0-1</td> <td>1-2</td> <td>2-4</td> <td>4-6</td> <td>6-9</td> <td>9-12</td> </tr> <tr> <td>$b - a$</td> <td>1</td> <td>1</td> <td>2</td> <td>2</td> <td>3</td> <td>3</td> </tr> <tr> <td>No of artefacts</td> <td>22</td> <td>15</td> <td>44</td> <td>37</td> <td>52</td> <td>58</td> </tr> <tr> <td>$P(a \leq X < b)$</td> <td>$\frac{1}{12}$</td> <td>$\frac{1}{12}$</td> <td>$\frac{1}{6}$</td> <td>$\frac{1}{6}$</td> <td>$\frac{1}{4}$</td> <td>$\frac{1}{4}$</td> </tr> <tr> <td>$228 \times P(a \leq X < b)$</td> <td>19</td> <td>19</td> <td>38</td> <td>38</td> <td>57</td> <td>57</td> </tr> </table> <table border="1" data-bbox="220 611 967 1039"> <thead> <tr> <th>Class</th> <th>O_i</th> <th>E_i</th> <th>$\frac{(O_i - E_i)^2}{E_i}$</th> <th>$\frac{O_i^2}{E_i}$</th> </tr> </thead> <tbody> <tr> <td>0-1</td> <td>22</td> <td>19</td> <td>$\frac{9}{19} = 0.4736\dots$</td> <td>25.57...</td> </tr> <tr> <td>1-2</td> <td>15</td> <td>19</td> <td>$\frac{16}{19} = 0.8421\dots$</td> <td>11.84...</td> </tr> <tr> <td>2-4</td> <td>44</td> <td>38</td> <td>$\frac{36}{38} = 0.9473\dots$</td> <td>50.94...</td> </tr> <tr> <td>4-6</td> <td>37</td> <td>38</td> <td>$\frac{1}{38} = 0.0263\dots$</td> <td>36.02...</td> </tr> <tr> <td>6-9</td> <td>52</td> <td>57</td> <td>$\frac{25}{57} = 0.4385\dots$</td> <td>47.43...</td> </tr> <tr> <td>9-12</td> <td>58</td> <td>57</td> <td>$\frac{1}{57} = 0.0175\dots$</td> <td>59.01...</td> </tr> </tbody> </table> <p data-bbox="220 1043 847 1077">H_0: <u>continuous uniform</u> distribution <u>is</u> a good fit</p> <p data-bbox="220 1079 895 1113">H_1: <u>continuous uniform</u> distribution <u>is not</u> a good fit</p> <p data-bbox="220 1126 1326 1211">$\sum \frac{(O_i - E_i)^2}{E_i} = \frac{313}{114} = 2.75$ or $\sum \frac{O_i^2}{E_i} - 228 = 230.745\dots - 228 = \dots$ (awrt 2.75)</p> <p data-bbox="220 1223 379 1256">$\nu = 6 - 1 = 5$</p> <p data-bbox="220 1267 1310 1312">$\chi^2_5(0.05) = 11.070$ (ft their ν i.e. $\chi^2_\nu(0.05)$)</p> <p data-bbox="220 1323 831 1357">2.75 < 11.070, insufficient evidence to reject H_0</p> <p data-bbox="220 1368 887 1402">Continuous uniform distribution is a suitable model</p>						Distance from centre of site (m)	0-1	1-2	2-4	4-6	6-9	9-12	$b - a$	1	1	2	2	3	3	No of artefacts	22	15	44	37	52	58	$P(a \leq X < b)$	$\frac{1}{12}$	$\frac{1}{12}$	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{4}$	$\frac{1}{4}$	$228 \times P(a \leq X < b)$	19	19	38	38	57	57	Class	O_i	E_i	$\frac{(O_i - E_i)^2}{E_i}$	$\frac{O_i^2}{E_i}$	0-1	22	19	$\frac{9}{19} = 0.4736\dots$	25.57...	1-2	15	19	$\frac{16}{19} = 0.8421\dots$	11.84...	2-4	44	38	$\frac{36}{38} = 0.9473\dots$	50.94...	4-6	37	38	$\frac{1}{38} = 0.0263\dots$	36.02...	6-9	52	57	$\frac{25}{57} = 0.4385\dots$	47.43...	9-12	58	57	$\frac{1}{57} = 0.0175\dots$	59.01...	<p>M1</p> <p>A1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>dM1A1</p> <p>B1</p> <p>B1ft</p> <p>M1</p> <p>A1</p> <p style="text-align: right;">12</p>
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<p>1st M1 for calculation of at least 3 widths and attempting proportions/probs. <u>or</u> for 1:2:3 ratio seen</p> <p>1st A1 for correct probabilities</p> <p>2nd A1 for all correct expected frequencies</p> <p>2nd M1 for attempting $\frac{(O - E)^2}{E}$ or $\frac{O^2}{E}$, at least 3 correct expressions or values.</p> <p>Follow through their E_i provided they are not all = 38</p> <p>3rd A1 for a correct set of calcs - 3rd or 4th column. (2 dp or better and allow e.g. 0.94...)</p> <p>3rd dM1 dependent on 2nd M1 for attempting a correct sum or calculation (must see at least 3 terms and +)</p> <p style="text-align: center;">The first three Ms and As can be implied by a test statistic of awrt 2.75</p> <p>4th M1 for a correct statement based on their test statistic (> 1) and their cv (> 3.8)</p> <p>Contradictory statements score M0 e.g. “significant” do not reject H_0.</p> <p>5th A1 for a correct comment suggesting that continuous uniform model is suitable. No ft</p>																																																																													

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Q7	(a) Label full time staff 1-6000, part time staff 1-4000 Use random numbers to select Simple random sample of 120 full time staff and 80 part time staff	M1 M1 A1 (3)
	(b) Enables estimation of statistics / errors for each strata <u>or</u> “reduce variability” <u>or</u> “more representative” <u>or</u> “reflects population structure” NOT “more accurate”	B1 (1)
	(c) $H_0: \mu_f = \mu_p, \quad H_1: \mu_f \neq \mu_p$ (accept μ_1, μ_2) $\text{s.e.} = \sqrt{\frac{21}{80} + \frac{19}{80}}, \quad z = \frac{52 - 50}{\sqrt{\frac{21}{80} + \frac{19}{80}}} = (2\sqrt{2})$ $= 2.828\dots$ (awrt 2.83)	B1 M1,M1 A1
	Two tailed critical value $z = 2.5758$ (or prob of awrt 0.002 (<0.005) or 0.004 (<0.01)) [2.828 > 2.5758 so] significant evidence to reject H_0 There is evidence of a difference in policy awareness between full time and part time staff	B1 dM1 A1ft (7)
	(d) Can use mean full time and mean part time ~ Normal	B1 B1 (2)
	(e) Have assumed $s^2 = \sigma^2$ or variance of sample = variance of population	B1 (1)
	(f) $2.53 < 2.5758$, not significant <u>or</u> do not reject H_0 So there is insufficient evidence of a difference in mean awareness	M1 A1ft (2)
	(g) Training course has closed the gap between full time staff and part time staff’s mean awareness of company policy.	B1 (1)
		17
	(a) 1 st M1 for attempt at labelling full-time and part-time staff. One set of correct numbers. 2 nd M1 for mentioning use of random numbers 1 st A1 for s.r.s. of 120 full-time and 80 part-time	
	(c) 1 st M1 for attempt at s.e. - condone one number wrong . NB correct s.e. = $\sqrt{\frac{1}{2}}$ 2 nd M1 for using their s.e. in correct formula for test statistic. Must be $\frac{\pm(52 - 50)}{\sqrt{\frac{p}{q} + \frac{r}{s}}}$ 3 rd dM1 dep. on 2nd M1 for a correct statement based on their normal cv and their test statistic 2 nd A1 for correct comment in context. Must mention “scores” or “policy awareness” and types of “staff”. Award A0 for a one-tailed comment. Allow ft	
	(d) 1 st B1 for mention of mean(s) <u>or</u> use of \bar{X} , provided \bar{X} clearly refers to full-time or part-time 2 nd B1 for stating that distribution can be assumed normal e.g. “mean score of the test is normally distributed” gets B1B1	
	(f) M1 for correct statement (may be implied by correct contextualised comment) A1 for correct contextualised comment. Accept “no difference in mean scores”. Allow ft	
	(g) B1 for correct comment in context that implies training was effective. This must be supported by their (c) and (f). Condone one-tailed comment here.	