

Centre No.					
Candidate No.					

Paper Reference					
<b>4</b>	<b>4</b>	<b>0</b>	<b>0</b>	<b>/</b>	<b>4 H</b>

Surname	Initial(s)
Signature	

Paper Reference(s)

**4400/4H**

**London Examinations IGCSE**  
**Mathematics**

Paper 4H

**Higher Tier**

Tuesday 11 May 2004 – Morning

Time: 2 hours

Examiner's use only

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Team Leader's use only

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**Materials required for examination**

Ruler graduated in centimetres and millimetres, protractor, compasses, pen, HB pencil, eraser, calculator. Tracing paper may be used.

**Items included with question papers**

Nil

Page Numbers	Leave Blank
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16	
Total	

**Instructions to Candidates**

In the boxes above, write your centre number and candidate number, your surname, initial(s) and signature.

The paper reference is shown at the top of this page. Check that you have the correct question paper.

Answer **ALL** the questions in the spaces provided in this question paper.

Show all the steps in any calculations.

**Information for Candidates**

There are 16 pages in this question paper. All blank pages are indicated.

The total mark for this paper is 100. The marks for parts of questions are shown in round brackets: e.g. (2).

You may use a calculator.

**Advice to Candidates**

Write your answers neatly and in good English.

Printer's Log. No.

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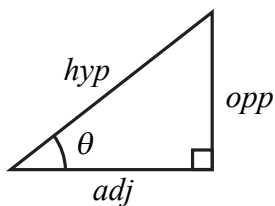
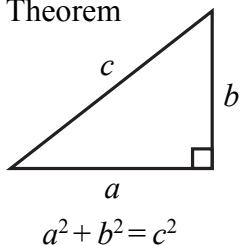
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**IGCSE MATHEMATICS 4400**  
**FORMULA SHEET – HIGHER TIER**

Pythagoras' Theorem

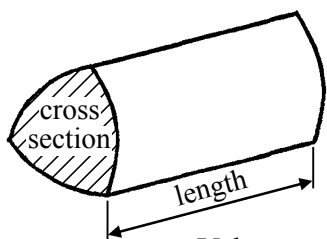


adj = hyp  $\times$  cos  $\theta$   
 opp = hyp  $\times$  sin  $\theta$   
 opp = adj  $\times$  tan  $\theta$

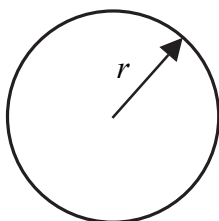
or  $\sin \theta = \frac{\text{opp}}{\text{hyp}}$

$\cos \theta = \frac{\text{adj}}{\text{hyp}}$

$\tan \theta = \frac{\text{opp}}{\text{adj}}$

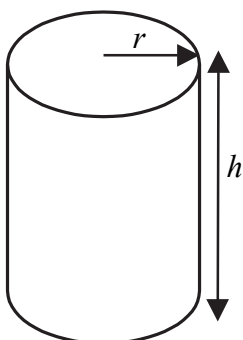


Volume of prism = area of cross section  $\times$  length



Circumference of circle =  $2\pi r$

Area of circle =  $\pi r^2$

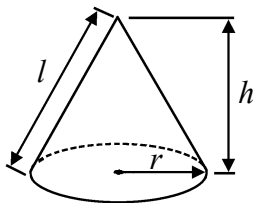


Volume of cylinder =  $\pi r^2 h$

Curved surface area of cylinder =  $2\pi r h$

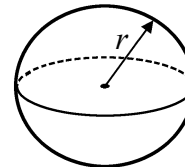
Volume of cone =  $\frac{1}{3} \pi r^2 h$

Curved surface area of cone =  $\pi r l$

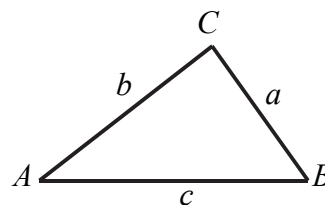


Volume of sphere =  $\frac{4}{3} \pi r^3$

Surface area of sphere =  $4\pi r^2$



In any triangle ABC

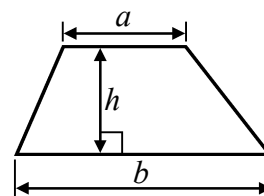


Sine rule  $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

Cosine rule  $a^2 = b^2 + c^2 - 2bc \cos A$

Area of triangle =  $\frac{1}{2} ab \sin C$

Area of a trapezium =  $\frac{1}{2} (a + b) h$



The Quadratic Equation

The solutions of  $ax^2 + bx + c = 0$  where  $a \neq 0$ , are given by

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

**Answer ALL TWENTY TWO questions.**

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blank*

**Write your answers in the spaces provided.**

**You must write down all stages in your working.**

1. Work out the value of  $\frac{6.1+3.4}{5.7-1.9}$

**Q1**

.....  
**(Total 2 marks)**

2. Suhail cycles 117 km in 4 hours 30 minutes.  
Work out his average speed in km/h.

**Q2**

..... km/h

**(Total 3 marks)**

3. The word formula gives the time, in minutes, needed to cook a turkey.

$$\text{Time} = 40 \times \text{weight in kg} + 20$$

A time of  $T$  minutes is needed to cook a turkey with a weight of  $W$  kg.

Write down a formula for  $T$  in terms of  $W$ .

**Q3**

.....  
**(Total 2 marks)**

4. The mean height of a group of 4 girls is 158 cm.

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blank*

(a) Work out the total height of the 4 girls.

..... cm  
**(1)**

Sarah joins the group and the mean height of the 5 girls is 156 cm.

(b) Work out Sarah's height.

..... cm  
**(3)**

**Q4**

**(Total 4 marks)**

5. Plumbers' solder is made from tin and lead.

The ratio of the weight of tin to the weight of lead is 1 : 2

(a) Work out the weight of tin and the weight of lead in 120 grams of plumbers' solder.

tin ..... g

lead ..... g  
**(2)**

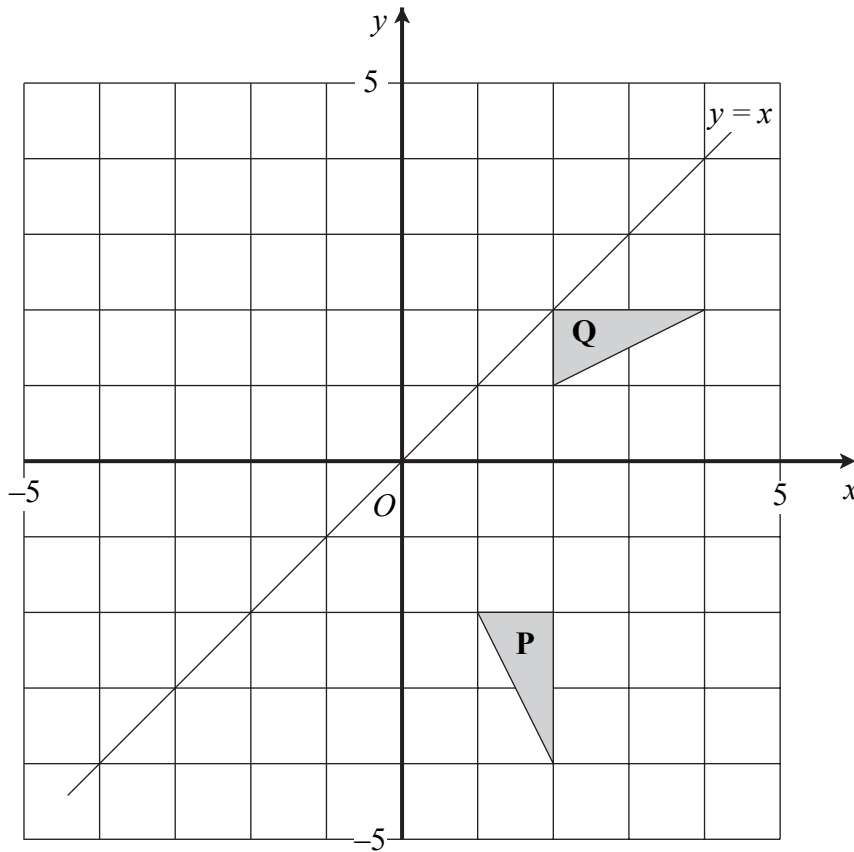
(b) What weight of plumbers' solder contains 25 grams of tin?

..... g  
**(1)**

**Q5**

**(Total 3 marks)**

6.



Leave blank

(a) Describe fully the single transformation which maps triangle **P** onto triangle **Q**.

.....  
.....

(3)

(b) Reflect triangle **Q** in the line with equation  $y = x$ .

(2)

Q6

(Total 5 marks)

7. Work out  $2\frac{2}{5} \times 1\frac{7}{8}$

Give your answer as a mixed number in its simplest form.

Q7

(Total 3 marks)

8. This formula is used in science.

$$v = \sqrt{2gh}$$

Leave  
blank

- (a) Hanif uses the formula to work out an estimate for the value of  $v$  without using a calculator when  $g = 9.812$  and  $h = 0.819$

Write down approximate values for  $g$  and  $h$  that Hanif could use.

approximate value for  $g$  .....

approximate value for  $h$  .....

(2)

- (b) Make  $h$  the subject of the formula  $v = \sqrt{2gh}$

$h =$  .....

(2)

Q8

(Total 4 marks)

9. (a) Simplify  $n \times n \times n \times n$

.....  
(1)

- (b) Simplify  $p^2 \times p^5$

.....  
(1)

- (c) Simplify  $\frac{q^7}{q^3}$

.....  
(1)

- (d) Simplify  $\frac{t^4 \times t^7}{t^8}$

.....  
(1)

Q9

(Total 4 marks)

10.

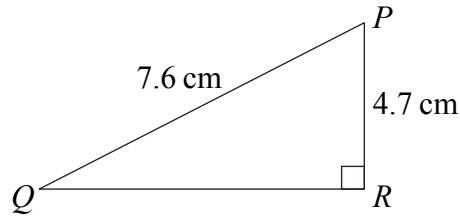


Diagram **NOT** accurately drawn

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Triangle  $PQR$  is right-angled at  $R$ .  
 $PR = 4.7$  cm and  $PQ = 7.6$  cm.

- (a) Calculate the size of angle  $PQR$ .  
Give your answer correct to 1 decimal place.

..... °  
.....  
**(3)**

The length, 7.6 cm, of  $PQ$  is correct to 2 significant figures.

- (b) (i) Write down the upper bound of the length of  $PQ$ .

..... cm

- (ii) Write down the lower bound of the length of  $PQ$ .

..... cm  
**(2)**

**Q10**

**(Total 5 marks)**

11. Solve  $4(x - 3) = 7x - 10$

$x =$  .....

**Q11**

**(Total 3 marks)**

12.

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blank*

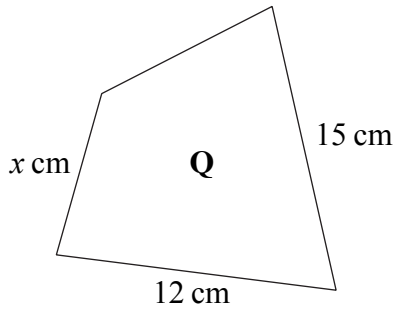
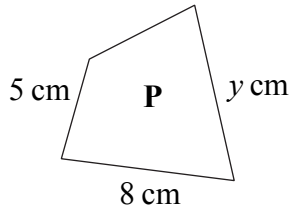


Diagram **NOT**  
accurately drawn

Quadrilateral **P** is mathematically similar to quadrilateral **Q**.

(a) Calculate the value of  $x$ .

$x = \dots\dots\dots$   
(2)

(b) Calculate the value of  $y$ .

$y = \dots\dots\dots$   
(2)

The area of quadrilateral **P** is  $60 \text{ cm}^2$ .

(c) Calculate the area of quadrilateral **Q**.

$\dots\dots\dots \text{ cm}^2$   
(2)

**Q12**

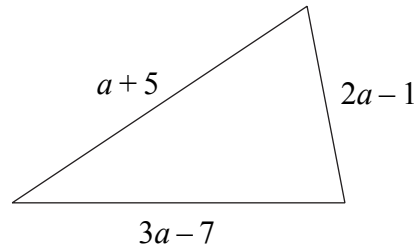
**(Total 6 marks)**

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13.

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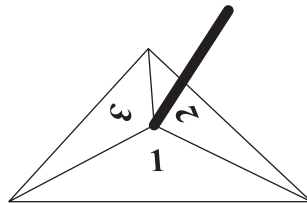
The lengths, in cm, of the sides of a triangle are  $(a+5)$ ,  $(3a-7)$  and  $(2a-1)$ .  
The perimeter of the triangle is 24 cm.  
Work out the value of  $a$ .

$a = \dots\dots\dots$

Q13

(Total 3 marks)

14. Here is a fair 3-sided spinner.



Its sides are labelled 1, 2 and 3 as shown.

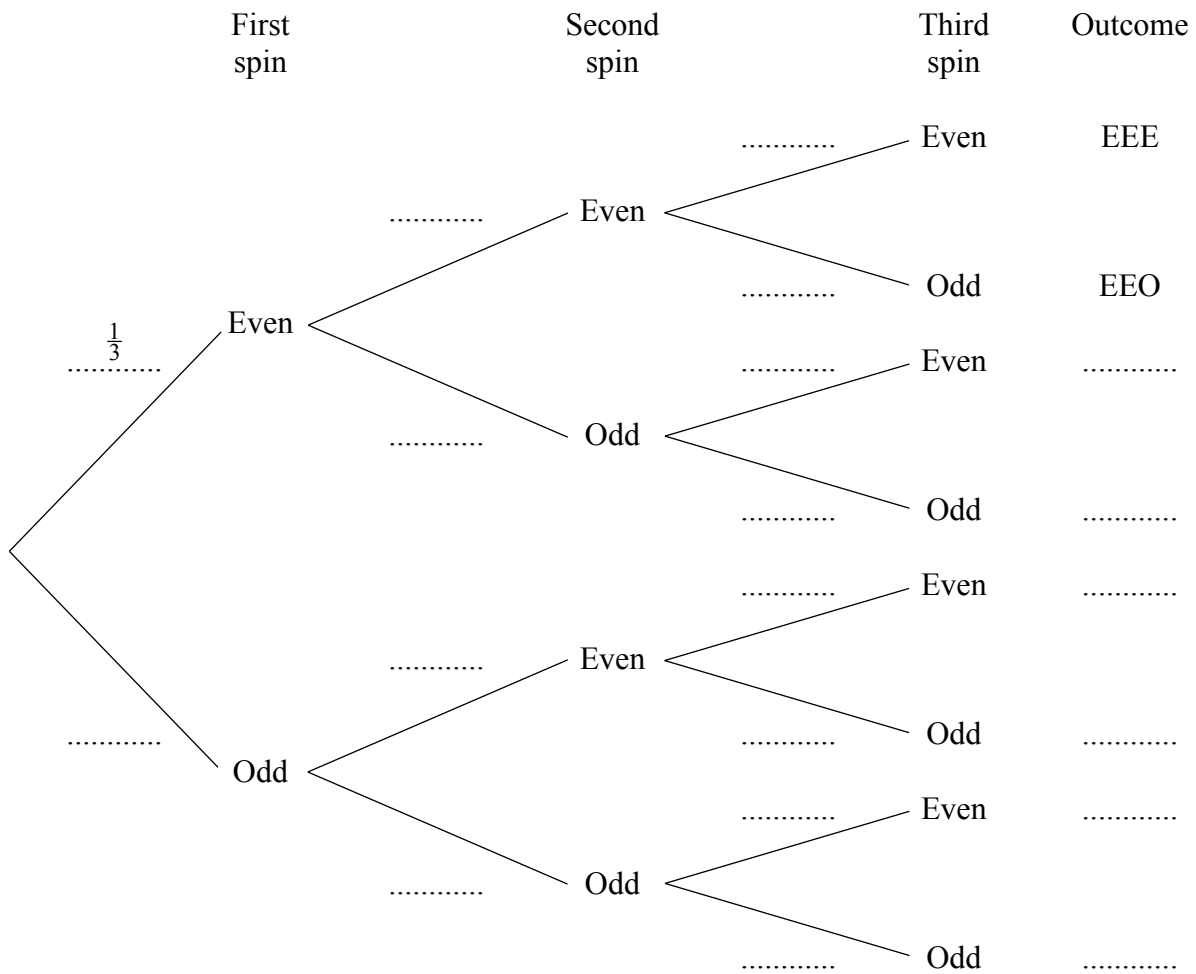
- (a) Aisha is going to spin the spinner twice.  
Work out the probability that it will land on 1 both times.

$\dots\dots\dots$   
(2)

Leave blank

(b) Harry is going to spin the spinner 3 times.

(i) Complete the probability tree diagram.



(ii) Work out the probability that the spinner will land on an odd number 3 times.

.....

(iii) Work out the probability that the spinner will land on an even number exactly once.

.....

(9) Q14

(Total 11 marks)

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15. In a sale, normal prices are reduced by 12%.  
The sale price of a computer is £726

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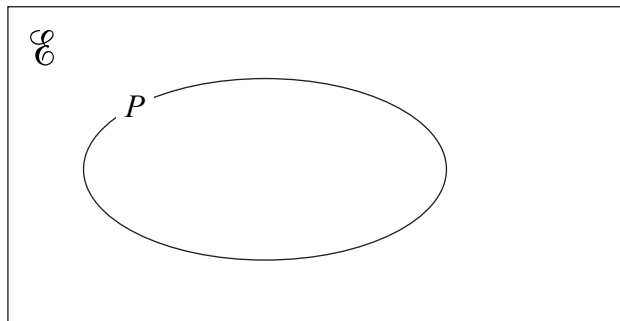
Work out the normal price of the computer.

£ .....

**Q15**

**(Total 3 marks)**

16.



Set  $P$  is shown on the Venn Diagram.  
Two sets,  $Q$  and  $R$ , are such that

$$R \subset P$$

$$Q \cap R = \emptyset$$

$$P \cup Q = P$$

Complete the Venn Diagram to show set  $Q$  and set  $R$ .

**Q16**

**(Total 3 marks)**

17. Convert the recurring decimal  $0.3\dot{2}$  to a fraction.

**Q17**

.....

**(Total 2 marks)**

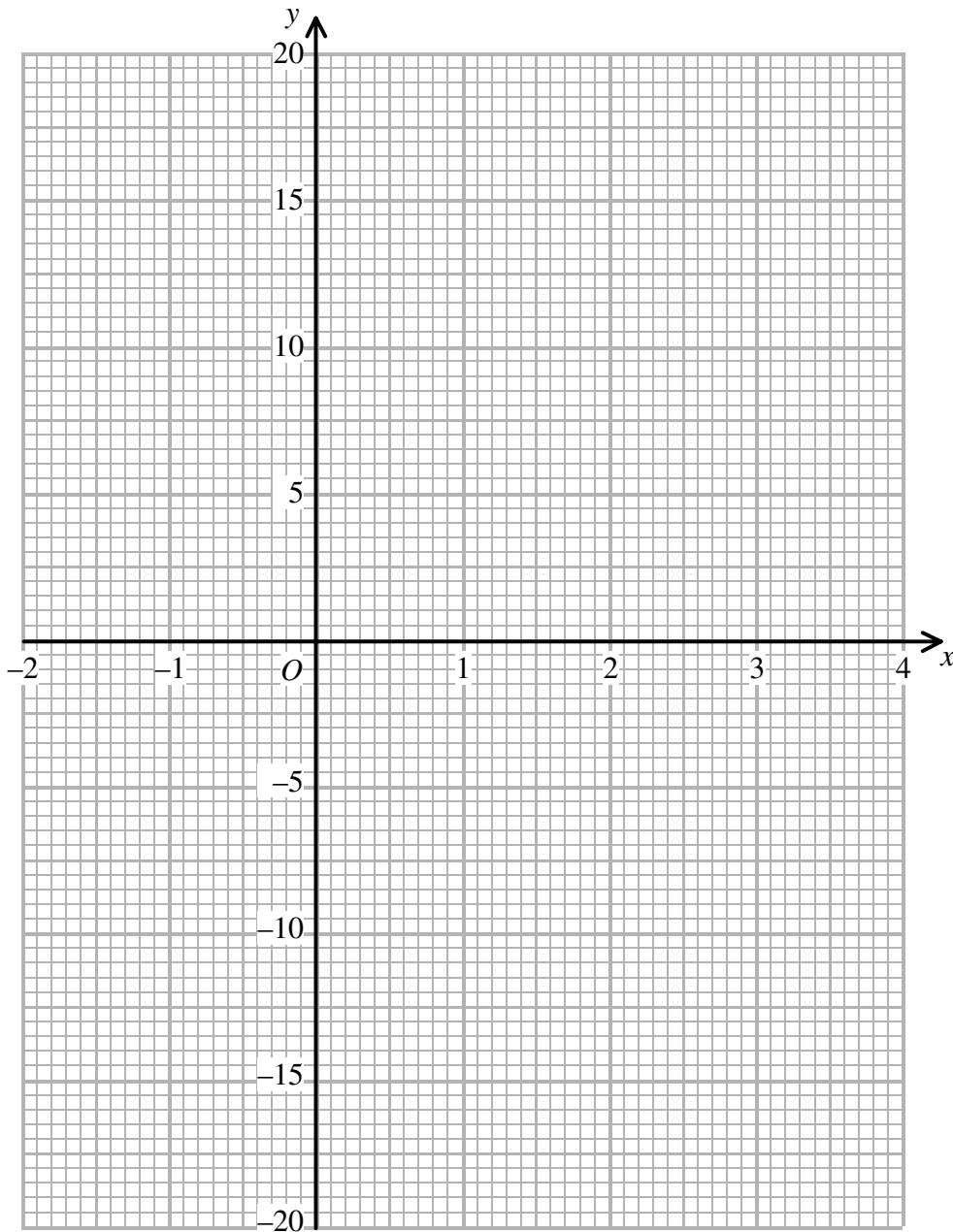
18. (a) Complete the table of values for  $y = x^3 - 3x^2 + 2$

$x$	-2	-1	0	1	2	3	4
$y$		-2					

(2)

Leave  
blank

(b) On the grid, draw the graph of  $y = x^3 - 3x^2 + 2$



(2)

(c) Use your graph to find estimates, correct to 1 decimal place where appropriate, for the solutions of

*Leave blank*

(i)  $x^3 - 3x^2 + 2 = 0$

.....

(ii)  $x^3 - 3x^2 - 4 = 0$

.....

(4)

**Q18**

**(Total 8 marks)**

**19.** (a) Expand and simplify  $(3p - 2q)(2p + 5q)$

.....

(2)

(b) Simplify  $(2x^2y^4)^3$

.....

(2)

(c) Simplify  $(a^4b^{-3})^{-2}$

.....

(2)

(d) Simplify  $(27p^6)^{\frac{1}{3}}$

.....

(2)

**Q19**

**(Total 8 marks)**

20.

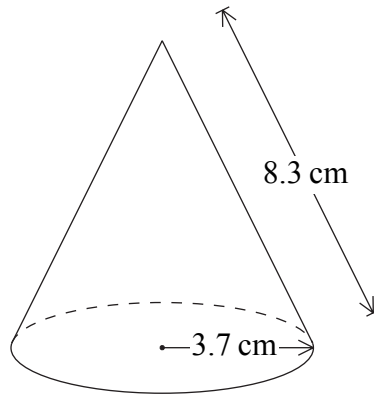


Diagram **NOT** accurately drawn

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The diagram shows a solid cone.  
The radius of its base is 3.7 cm and the slant height is 8.3 cm.

- (a) Calculate the total surface area of the cone.  
Give your answer correct to 3 significant figures.

..... cm<sup>2</sup>  
(2)

- (b) Calculate the volume of the cone.  
Give your answer correct to 3 significant figures.

..... cm<sup>3</sup>  
(4)

**Q20**

**(Total 6 marks)**

21. Solve the simultaneous equations

$$2x + y = 6$$

$$x^2 + y^2 = 20$$

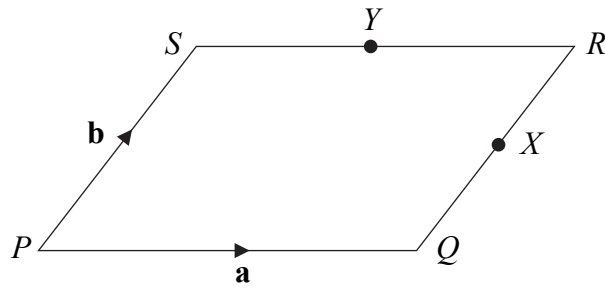
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Q21

(Total 7 marks)

22.

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blank



$PQRS$  is a parallelogram.  
 $X$  is the midpoint of  $QR$  and  $Y$  is the midpoint of  $SR$ .  
 $\vec{PQ} = \mathbf{a}$  and  $\vec{PS} = \mathbf{b}$ .

(a) Write down, in terms of  $\mathbf{a}$  and  $\mathbf{b}$ , expressions for

(i)  $\vec{PX}$

.....

(ii)  $\vec{PY}$

.....

(iii)  $\vec{QS}$

.....

(3)

(b) Use a vector method to show that  $XY$  is parallel to  $QS$  and that  $XY = \frac{1}{2}QS$ .

(2)

Q22

(Total 5 marks)

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TOTAL FOR PAPER: 100 MARKS

END